Abstract

Statistics are an almost unavoidable component of modern psychology and probability (or \( p \)) values are ubiquitous in published work. Despite this, many students hold misconceptions about what \( p \) values represent, some of which suggest a fundamental misunderstanding of the underlying theory. This study investigated whether it was possible to correct a specific misconception by showing participants a video that provided a detailed explanation of the correct interpretation of a \( p \) value. Scores on two measures of statistical knowledge suggested that the correction was ineffective. This study also found that repeating the misconception during correction had no effect on the efficacy of a correction. Challenges in correcting \( p \) value misconceptions are highlighted, including the key issue potentially being either an insufficiently detailed statistical education, or the complexity of the underlying theory. Implications for statistical education are discussed and Bayesian methods are proposed as a simpler alternative in psychological research and undergraduate education.
Broadly speaking, scientific investigation can be split into theoretical ideas and practical research. The latter includes how experiments are planned and conducted, and how the resulting data are analysed. Despite their importance, many undergraduate students do not enjoy learning these practical elements (Murtonen, 2005; Murtonen & Lehtinen, 2003), preferring instead to learn the theoretical ideas that underpin experiments (Vittengl et al., 2004).

Learning statistical methods is often regarded as the least enjoyable component of undergraduate psychology programmes (Addison, Stowell, & Reab, 2015), and students even report statistics courses to be anxiety-inducing (Hanna, Shevlin, & Dempster, 2008; Macher, Papousek, Ruggeri, & Paechter, 2015). Unsurprisingly, this leaves students with a weak grasp of statistical concepts (Macher et al., 2015). This a major concern given that the majority of modern psychological investigations include statistics. It is therefore essential that students graduate with a solid understanding of how to interpret them.

A starter in statistics

By far the most prevalent school of statistical analysis in psychology is frequentist, taught in almost all universities and reported in almost all published papers (Hubbard & Ryan, 2000). Frequentist methods were developed in the early 20th century by notable mathematicians such as Egon Pearson, Jerzy Neyman and Ronald Fisher, in an attempt to provide previously anecdotal sciences with methodological rigour (Perezgonzalez, 2015).

The majority of statistical tests in psychology are null hypothesis significance tests. The result of which is a probability (or \( p \)) value, representing the probability of observing a result given that the null hypothesis is true (Hubbard & Armstrong, 2006). \( P \) values are the most prevalent statistic in published work, with 94% of published psychological papers reporting at least one (Hubbard & Ryan, 2000).

The inferential utility of \( p \) values is dependent on many factors including sample size and effect size (Ziliak & McCloskey, 2008). However, results are often judged to have merit solely on the statistical significance of a \( p \) value, and many authors fail to report other crucial results (Fritz, Scherndl, & Kühberger, 2013; Kühberger, Fritz, Lermer, & Scherndl, 2015). This is dangerous practice, as \( p \) values by themselves are a relatively uninformative measure (Armstrong, 2007; Kline, 2013).

Despite their prevalence, \( p \) values have always been marked by issues, both theoretical and practical (Benjamin et al., 2018; Wagenmakers, Lee, Lodewyckx, & Iverson, 2008; Wagenmakers, Marsman, et al., 2018). One of these practical issues is the prevalence of misconceptions (false ideas or beliefs) regarding what \( p \) values represent and how they should be interpreted (Cohen, 1994; Kirk, 2001).

Misconception prevalence

Replicated findings show that 90% of psychologists hold at least one misconception regarding what \( p \) values represent (Haller & Krauss, 2002). Even statistics textbooks and 80% of statistics teachers have been found to hold misconceptions, making it likely that they will be passed on to students (Badenes-Ribera & Navarro, 2017; Gigrenzer, Krauss, & Vitouch, 2004; Gliner, Morgan, Leech, & Harmon, 2001; Haller & Krauss, 2002; Lecoutre, Poitievineau, & Lecoutre, 2003). Misconceptions are even more problematic when they make it into published work. Findings suggest that up to 18% of reputable journal articles contain incorrectly reported statistics (Bakker & Wicherts, 2011). Incorrect statistics lead to inappropriate conclusions which seriously damage the integrity of the literature and
are a key contributor to the field’s current replication crisis (Aarts et al., 2015).

Misconceptions are most prevalent in undergraduate students. One study found that all 44 students tested held at least one of six misconceptions, with some students holding multiple incorrect views as to what a $p$ value represents (Haller & Krauss, 2002). $P$ values are by no means the only component of hypothesis testing subject to misconceptions (Chance, del Mas, & Garfield, 2004; Lipson, 2002; Sotos, Vanhoof, Van den Noortgate, & Onghena, 2007). However, given the prevalence and influence of $p$ values, this is an issue which warrants attention.

Misconception content

Many different misconceptions regarding $p$ values exist (Goodman, 2008). The following two are understood to be among the most common (Kline, 2013), with $p$ values being (incorrectly) interpreted as the probability that:

1) The results are due to chance;
2) The research hypothesis is true.

Both of these interpretations are incorrect. A $p$ value represents the probability of observing the data given the null hypothesis is true. The first of these misconceptions is regarded as being the most prevalent (Carver, 1978; Kline, 2013), however the second misconception is likely to be the most damaging.

Paradoxically, frequentist hypothesis tests tell us nothing about the probability of hypotheses. Instead, they report the probability of observing the data given the hypothesis, a subtle but important difference (Wagenmakers et al., 2008). Thinking that a $p$ value represents the probability of a hypothesis being true (or false) is a fundamental misunderstanding of the theory that underlies the method.

Up to 59% of undergraduate students believe this misconception (Haller & Krauss, 2002). Given the prevalence of $p$ values in psychological research, it is concerning that so many students demonstrate such a profound misunderstanding of what they represent. To date, relatively few studies have attempted to correct $p$ value misconceptions (Khazanov & Prado, 2010; Krauss & Wassner, 2002). Fortunately, a wealth of literature on correcting misconceptions already exists.

Correcting misconceptions

Part of the challenge in communicating a correct interpretation of a $p$ value is its complexity, with understanding requiring the integration of many abstract ideas (Sotos et al., 2007). Humans have a bias towards believing simple explanations, increasing the risk of misconceptions when communicating complicated ideas (Chater & Vitanyi, 2003; Lombrozo, 2007; Pacer & Lombrozo, 2017). However, it is possible to overcome this bias by providing participants with a detailed understanding of why misconceptions are incorrect (Kowalski & Taylor, 2009; Weisman & Markman, 2017).

Much of the existing literature on correcting misconceptions looks to change only a single fact or an incorrect headline, limiting its use in the current context (Chan, Jones, Jamieson, & Albarracin, 2017). The literature does, however, highlight three important considerations in devising and delivering an effective correction: narrative coherence, backfire effects, and repetition.

Narrative coherence

Participants likely hold internal narratives which structure their knowledge and therefore contain any misconceptions (Johnson & Seifert, 1994). To enable a complex idea to replace a misconception, the information needs to fit into a coherent narrative (Johnson & Seifert, 1994; Johnson-Laird, 2012; Schwarz, Sanna, Skurnik, & Yoon, 2007). If a correction changes facts but does not provide a coherent narrative, participants are more likely to rely on their previous misconception, even if they know it to be
false (Gerrie, Belcher, & Garry, 2006; Johnson & Seifert, 1994).

Providing an alternate narrative is more effective than disputing facts (Tenney, Cleary, & Spellman, 2009), and allowing participants to reason through cognitive conflicts and see why a misconception cannot be correct is also beneficial (Khazanov & Prado, 2010; Rapp & Kendeou, 2007; Seifert, 2002). Given that the correct interpretation of a p value is the only true interpretation, there is a coherent narrative behind it. The challenge is communicating this simply and with sufficient detail.

**Backfire effects**

Backfire effects arise when an attempted correction paradoxically *increases* the strength of a misconception in a participant’s mind (Lewandowsky, Ecker, Seifert, Schwarz, & Cook, 2012; Peter & Koch, 2016). Backfire effects would mark an attempted correction as a grievous failure and it is therefore essential that they are avoided.

Theories as to why backfire effects exist suggest that entrenched ideological beliefs cause participants to think that views that require challenging must be credible (Nyhan & Reifler, 2010). Such concerns are unlikely to affect the issue at hand as students – whilst not liking statistics – probably do not have strong ideological beliefs about what p values represent. Of more relevance, backfire effects can arise when corrections are too complicated for participants to understand. This highlights the need for a coherent correction (Chan et al., 2017). Indeed, there is evidence to show that corrections can be effective – and backfire effects minimal – when information is presented clearly (Wood & Porter, 2019).

With these two issues in mind, the correction used in this study is based on providing a detailed and coherent narrative of what a p value represents. This is similar to how statistics are taught in the first instance, meaning that if the correction is successful, implementation in education is realistic.

**Repetition**

A final consideration is whether or not the misconception is repeated during the correction. Many studies find that repeating the misconception (even whilst correcting it) strengthens belief in it, as the information seems more familiar (Eakin, Schreiber, & Sergent-Marshall, 2003; Ecker, Lewandowsky, Swire, & Chang, 2011; Lewandowsky et al., 2012).

However, avoiding repetition of the misconception may lead participants to become confused as to what the correction relates to (Chan et al., 2017). Therefore, it may be necessary to repeat the misconception when providing a detailed correction. There is also evidence to show that the negative effects of repetition can be avoided if the misconception is refuted as it is mentioned (Cook & Lewandowsky, 2011).

The present study investigates the effect of repetition by using two experimental conditions: one which repeats and immediately refutes the misconception, and one that does not repeat the misconception at all.

**The present study**

This study investigated whether it was possible to correct a misconception by showing participants a detailed video explanation of the correct interpretation of a p value. The video showed a statistics teacher and accompanying slides and was chosen to be analogous to classroom learning, therefore more representative of how students learn statistics. In addition, video supplements are increasingly popular in education (Gedera & Zalipour, 2018; McGarr, 2009), and there is evidence to suggest that video is a more effective medium for communicating information than writing (Wilson et al., 2012; Wilson et al., 2010).

The present study aims to correct the misconception that a p value represents the
probability of the research hypothesis being true. This misconception is especially prevalent in students and demonstrates a crucial misunderstanding of the underlying statistical theory. The correction aims to provide a detailed explanation of what a $p$ value represents and why, enabling participants to understand why the misconception is incorrect.

**H1** – *Participants shown a corrective video will score higher on tests of statistical knowledge than those not shown a corrective video.*

I also investigated the effect of repeating the misconception on the efficacy of a correction. Given that the correction is detailed, I did not expect backfire effects to be present. However, in line with the literature, I expected that the correction with repetition would be less effective than the correction without repetition.

**H2** – *Participants shown a corrective video that repeats the misconception will score lower on tests of statistical knowledge than participants shown a corrective video that does not repeat the misconception.*

**Method**

**Design**

This is a between-subjects design with one independent variable (condition: Control, No repetition, Repetition), and two dependent variables that measure statistical knowledge. This study was implemented as part of a larger study which included two additional conditions and two additional dependent variables. Each participant completed one condition and all four dependent measures.

**Participants**

A frequentist *a priori* power analysis was conducted using G*Power (Faul, Erdfelder, Lang, & Buchner, 2007), based on the results of a meta-analysis which reported an effect size of between $d = 1.14 – 1.33$ for the correction of misinformation (Chan et al., 2017). Given the sheer magnitude of this effect and the tendency for reported effects to be inflated (Aarts et al., 2015; Bakker, van Dijk, & Wicherts, 2012), a more conservative estimate of effect size ($d = 0.6$) was used. With alpha level .05 and power of .8, a target sample size of 36 participants per condition was obtained, for a total of 108.

Due to time limitations and in accordance with the stopping rules specified in the pre-registration (https://osf.io/7gex9/), a total of 88 participants completed the study, all of whom were psychology students at The University of Bristol. Due to the lower participant numbers, a sensitivity power analysis was conducted using G*Power to determine the minimum detectable effect (MDE) that could be observed for each of the comparisons. This yielded an MDE of $d = 0.56$ for the comparison between control and experimental conditions, and $d = 0.67$ for the comparison between the two experimental conditions.

Those in the first and second year of their undergraduate degree completed the experiment in exchange for course credit. Others were not reimbursed for their time. Full demographic information can be seen in Table 1.

<table>
<thead>
<tr>
<th>Table 1. Demographic information for each condition</th>
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</thead>
<tbody>
<tr>
<td>Condition</td>
</tr>
<tr>
<td>-------------</td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td>Control</td>
</tr>
<tr>
<td>No repetition</td>
</tr>
<tr>
<td>Repetition</td>
</tr>
<tr>
<td>Total</td>
</tr>
</tbody>
</table>
Materials and Measures

The experiment centred around a fictional news report which described a fictional study conducted in the Netherlands. This tested the effect of reintroducing wild animal species on the number of flood days per year in 24 rural areas. The full article can be seen in the online supplement (https://osf.io/7gex9/). The report was designed to simply outline the structure of a frequentist independent samples t-test. The report highlights that the researchers’ investigation yields a result significant at the $p<.05$ level. Crucially, the researchers (incorrectly) conclude that a $p$ value corresponds to the probability of the research hypothesis being true.

Independent variable

In order to correct the misconception, two short videos were produced. These involved a well-known statistics teacher at The University delivering a script whilst a simple graphic beside him illustrated how a statistical result derived from a sample corresponds to the distribution of differences in a population (see Figure 1). The statistics teacher was used in order to provide the correction with credibility.

The script for these videos was written to correct the misinterpretation of the $p$ value presented in the text. The two scripts differed only in whether or not they repeated the misconception from the text whilst correcting it. The No repetition script did not repeat the misconception whilst the Repetition script repeated it four times (see online supplement).

Figure 1. Screenshots from the corrective videos.
Dependent variables
The first dependent variable was a single open question, asking ‘How should a \( p \) value be interpreted?’. This was designed to test participants’ knowledge of \( p \) values outside of the strict context encountered in the experiment. There was no minimum or maximum word count.

The answers to this question were analysed by three raters (including the author) and scored from 0 – 3. To make the analysis as transparent and objective as possible, a keyword marking system was used whereby answers were awarded one mark for including each of the following three phrases (or variations of them): ‘the probability of’, ‘observing these results’, ‘given the null hypothesis is true’. The three raters independently rated answers and then discussed any inconsistencies to reach a single set.

As a separate analysis, answers were also classified by the raters into three open question groups depending on whether answers were 1) unambiguously correct, 2) repeated the misconception from the article, or 3) either evidenced a different misconception or were incorrect.

The second dependent variable was participants’ score on six closed ended sentence completion questions. Participants saw the sentence stem from the initial article and clicked to select whether each presented ending represented a correct (2/6) or incorrect (4/6) interpretation of the researchers’ results. These were adapted from a previous study, and designed to specifically test four misconceptions (see Table 2) (Haller & Krauss, 2002). Each participant received a score out of six corresponding to how many questions they answered correctly.

Table 2.
The closed questions that formed the second dependent variable and the misconception each was designed to test

<table>
<thead>
<tr>
<th>Sentence ending</th>
<th>Misconception tested</th>
</tr>
</thead>
<tbody>
<tr>
<td>There is a less than 5% likelihood that rewilding had no effect on flood days.</td>
<td>( P ) is the probability of the null hypothesis being true.</td>
</tr>
<tr>
<td>These results were at least 95% likely to have occurred due to the rewilding project.</td>
<td>( P ) is the probability of the alternative hypothesis being true.</td>
</tr>
<tr>
<td>There is a less than 5% likelihood that accepting the effects of the rewilding project as true is the wrong decision.</td>
<td>( P ) is the probability of making a type I error.</td>
</tr>
<tr>
<td>If the rewilding experiment could be repeated 100 times, the result would be significant at the ( p &lt; .05 ) level 95 out of the 100 times.</td>
<td>( P ) is the probability of the same result being obtained through replication.</td>
</tr>
<tr>
<td>There was a less than 5% likelihood of these results having occurred even if the rewilding project had no effect.</td>
<td>Correct interpretation.</td>
</tr>
<tr>
<td>There was a less than 5% likelihood that something other than the rewilding project caused the reduction in the number of flood days.</td>
<td>Correct interpretation.</td>
</tr>
</tbody>
</table>

Note. Sentence prompt: ‘The researchers found that the rewilded areas experienced fewer flood days, a finding that was significant at the \( p < .05 \) level. This means that ________.’

(Adapted from Haller & Krauss, 2002).
Procedure

The experiment was delivered through the Qualtrics online platform (Qualtrics, 2019). Of the 88 participants, 79 came into the lab to do the experiment and 9 (three from each condition) took the experiment remotely on either a desktop or laptop in a push to increase sample size. Participants were instructed to wear the supplied headphones even though they may not need them. Participants were randomised into a condition by Qualtrics and instructions were provided through the software.

After proving demographic information and consent, participants read the article which contained the misconception. Participants in the two experimental conditions then saw a screen introducing the video and watched the video. The videos were 2:25 and 2:46 minutes long, for the No repetition and Repetition conditions respectively. Participants were free to rewind and skip through the video as they desired and the page auto-advanced after 4:00 minutes. All participants then answered several arithmetic questions as a short distractor task before the questions. These were not assessed and the page ensured participants spent between 1:30 and 2:00 minutes on the task.

Participants responded to four sets of questions: two open questions, and two banks of six closed questions. The open questions were shown first. The first asked them to complete the final sentence of the article so it represented a correct interpretation of the researchers’ results. The second question, as outlined in the dependent variables section, asked how a p value should be interpreted.

Within the two banks of closed questions, each of the six possible answers appeared on screen one at a time and in a randomised order. The first bank is shown in Table 2. The second bank of questions presented sentences and asked if each was a correct or incorrect interpretation of what a p value represents. Only the data from the second of the open questions and the first bank of the closed questions are reported here. The data from the other questions are reported in a separate study. The order of the question sets was not counterbalanced as this would have given some participants an advantage. Participants were then debriefed. The experiment took between 7.5 and 25 minutes, depending on condition. The study was approved by The University’s Research Ethics Committee (code: 80902).

Data analysis plan

As part of the effort to avoid misconceptions, the data here are analysed using Bayesian methods. A parallel, frequentist analysis is presented in the online supplement for comparison. The two analyses suggest similar conclusions.

The key hypothesis tests require a comparison of independent participant groups on two dependent measures. This is split into four Bayesian independent samples comparisons (analogous to independent samples t-tests), two for each dependent variable. The comparisons are the same for both dependent variables. The first compares the scores of the control condition to the average scores of both experimental conditions to test whether there is an effect of correction. The second compares the scores of the two experimental conditions to test whether there is an effect of repetition. For all four of these comparisons, a Bayes factor is presented. In addition, effect sizes and 95% credible intervals are provided. A Bayesian contingency table was also created as an exploratory measure to investigate how each condition affected the prevalence of the original misconception after correction.

It is worth noting that Bayesian comparisons do not need to correct for inflated error rates arising from multiple comparisons in the same way that frequentist methods do as Type I error does not exist in Bayesian analysis (Gelman, Hill, & Yajima, 2012).
Analysis

Two comparisons were conducted on open question score. The first was between the scores for the Control condition and the average of the two experimental conditions; the second comparison was between the two experimental conditions. The same comparisons were also conducted on closed question score, the second dependent variable.

All Bayesian comparisons used the default Cauchy prior width ($r = .707$), a conservative prior that slightly favours the null hypothesis (Rouder, Speckman, Sun, Morey, & Iverson, 2009; Wagenmakers, Love, et al., 2018). As tests were confirmatory, a directional hypothesis was used in all tests. It was hypothesised that on both dependent variables, the average score for the experimental conditions would be higher than the average for the Control condition, and that the average for the No repetition condition would be higher than that of the Repetition condition.

The result of a Bayesian analysis is a Bayes factor (BF) which represents the likelihood of a hypothesis given the observed data. All Bayes factors are reported as BF10s, representing the strength of evidence in favour of the research hypothesis. In line with the classification scale developed by Wagenmakers and colleagues (2018), BFs between .33 and 3 are seen as non-diagnostic and those between 3 and 10 represent moderate evidence in favour of the research hypothesis. BFs 10 to 30, 30 to 100, and >100 represent strong, very strong, and extreme evidence in favour of the research hypothesis respectively. In contrast, BFs .33 to .10, .10 to .03, .03 to .01, and <.01 represent moderate, strong, very strong, and extreme evidence in favour of the null hypothesis respectively. The Bayesian analysis was conducted using JASP 0.9.2 (JASP Team, 2019).

<table>
<thead>
<tr>
<th>Condition</th>
<th>Descriptive statistics</th>
<th>Comparisons</th>
<th>Open Question Scores</th>
<th>Closed Question Scores</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>N</td>
<td>M</td>
<td>SD</td>
<td>Mean difference</td>
</tr>
<tr>
<td>Control</td>
<td>31</td>
<td>0.71</td>
<td>0.86</td>
<td></td>
</tr>
<tr>
<td>Experimental</td>
<td>57</td>
<td>1.11</td>
<td>1.15</td>
<td>0.40</td>
</tr>
<tr>
<td>No repetition</td>
<td>28</td>
<td>0.96</td>
<td>1.07</td>
<td>-0.28</td>
</tr>
<tr>
<td>Repetition</td>
<td>29</td>
<td>1.24</td>
<td>1.22</td>
<td></td>
</tr>
<tr>
<td>Control</td>
<td>31</td>
<td>2.71</td>
<td>1.22</td>
<td></td>
</tr>
<tr>
<td>Experimental</td>
<td>57</td>
<td>3.11</td>
<td>1.26</td>
<td>0.40</td>
</tr>
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<td>No repetition</td>
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<td>1.32</td>
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<td>Repetition</td>
<td>29</td>
<td>3.24</td>
<td>1.22</td>
<td></td>
</tr>
</tbody>
</table>

Note. The BFs are placed in the row of the condition hypothesised to have the higher score.

Note. The mean differences for the two dependent variables are exactly the same. I am aware that this is more likely due to researcher error than chance (Abelson, 1995), and I have checked the data entry and analysis to ensure its legitimacy. Satisfied with the integrity of the outcome, I have made the raw data available at [https://osf.io/7gex9](https://osf.io/7gex9) for inspection should the reader wish to do the same.
Effect size $\partial$ is the standardised difference between two independent means (Cohen’s $d$ for the population) and the 95% credible interval represents a range we can be 95% confident that the true value of $\partial$ falls within. In calculating these, a non-directional hypothesis was used in order to allow the credible interval to span both sides of 0.

Bayes factors, effect sizes and credible intervals for each of the four pairwise comparisons are reported in full in Table 3. Mean scores on both dependent variables across the three conditions are presented in Figure 2. The prior and posterior distributions for all four comparisons can be seen in Figure 3, showing how estimates of the true population effect size were informed by both the default prior distribution used and the observed data.

Figure 2. Mean scores and credible intervals for open and closed questions across conditions.

Figure 3. Showing the prior and posterior distributions for each of the four pairwise comparisons, where effect size $\partial$ is shown on the X-axis and density is shown on the Y-axis.
Results
In sum, the comparisons between the control condition and the mean of both experimental conditions were non-diagnostic for both dependent variables. This suggests insufficient evidence to conclude that watching a corrective video does or does not improve participants’ performance on tests of p value knowledge.

For both dependent variables, there was moderate evidence in favour of the null hypothesis for the comparisons between the No repetition and Repetition conditions. A consultation of mean scores in Figure 2 suggests that the hypothesised effect may exist in the opposite direction, however the choice of directional hypotheses in this study prevents further comment. This suggests that repetition did not have an effect on the efficacy of misconception correction. For all comparisons, effect sizes were small and credible intervals were wide, supporting the non-diagnostic nature of the observed Bayes factors.

To assess the impact of condition on open question group, a Bayesian contingency table was constructed (equivalent to a frequentist chi-squared test). Overwhelmingly, participants in all conditions provided incorrect answers to the open question (see Figure 4).

The analysis yielded a Bayes factor of BF01 = 12.03, meaning the null hypothesis (that there is no difference between groups) was 12 times more likely than the alternative hypothesis.

Discussion
This study aimed to investigate the effect of corrective videos on the prevalence of a misconception about what a p value represents. This study found no diagnostic evidence to suggest that participants shown a corrective video demonstrated fewer misconceptions than those not shown a corrective video. This study also investigated the effect of repeating the misconception and found moderate evidence to suggest that the efficacy of a corrective video was not affected by repetition of the misconception.

The correction
Perhaps the most likely explanation for the failure to correct the misconception is the quality of the correction itself. Narrative coherence was the key objective in devising the correction and one which I believe to have been met. However, embedding the correction into a narrative makes it longer and it would be interesting to investigate whether the length of a correction affects efficacy.

Figure 4. Percentage breakdown of open question group by condition.
The correction was devised over a period of several weeks and involved lengthy discussion between six psychology students and a statistics teacher. The online supplement (https://osf.io/7gex9/) contains the correction in full and I welcome any comments on how it can be improved, without detracting from its statistical accuracy or brevity. Interestingly, trying to communicate this idea in a simple way was a real challenge, and may suggest that the inherent complexity of the subject matter is why misconceptions are so prevalent in textbooks (Gliner et al., 2001).

Another point to note is the number of participants who showed some form of misconception other than the one explicitly tested for (34.04%) (see Figure 4). This was relatively stable across conditions and may suggest that any correction needs to be tailored to the specific misconception held by students.

One potential limitation of this study is the use of a video correction. Recent results tentatively suggest that a written correction may be more effective (Peachey, 2019), and future work comparing the efficacy of different correction methods could better inform interventions. It is also worth noting that there was a difference between how the misconception and the correction were presented, in writing and as a video respectively. Future work could investigate whether the efficacy of corrections is higher when they are presented in the same medium as the misconception.

A definite limitation is the study’s low statistical power. The observed effect sizes were smaller than the minimum detectable effect gained from the sensitivity power analysis. This means that whilst the true population effect could be of the magnitude reported, the study is insufficiently powered to detect an effect this small. This could be remedied by testing more participants. If future work used Bayesian methods, the present results could be incorporated as a prior belief, providing a closer estimate of the true population effect (Wagenmakers, Marsman, et al., 2018).

Repetition

The repetition of the misconception during correction was hypothesised to make the correction less effective. The results of this study did not support this hypothesis, with the relationship appearing to exist in the opposite direction (see Figure 2). This suggests that repetition may not be a concern for detailed corrections. Such a finding is useful in informing interventions and is in line with existing evidence (Cook & Lewandowsky, 2011). However, it is possible that the effects of repetition were too small to be observed in this study simply because the correction worked on so few participants. It is therefore difficult to conclude on whether the efficacy of a correction is affected by repetition.

To my knowledge, this is the first study that seeks to correct misconceptions students hold about p values. Given the novelty of the research question and the low power of this study, these findings should not be taken to conclude that p value misconceptions cannot be corrected. Instead, this study can offer tentative suggestions about the nature of the issue and raise interesting points for future research.

Correction vs education

One important question is whether we should consider this an issue of misconception correction, or one of statistical education. As noted in the introduction, many important factors in correcting misconceptions are not relevant in the current context. Students don’t hold strong ideological beliefs surrounding p values nor are they under any obvious social pressure to continue believing misconceptions. In addition, undergraduates tend to have a weak grasp of statistics and scientific research methods in general, with most students seeing statistical analysis as process-driven (Rothman, 2014). In contrast, statistically
adept scientists need detailed knowledge of a range of useable methods, and good judgement concerning when to apply them (Krueger & Heck, 2019).

Therefore the issue may be that scientific education does not teach enough of the statistical theory underlying the interpretation of $p$ values, leaving students susceptible to fill their knowledge gaps with misconceptions. If $p$ value misconceptions are stubborn through students’ ignorance of the relevant theory, the challenge becomes teaching statistics simply and in enough detail that misconceptions cannot take root. 

**Education as antidote**

Students need to be able to recognise and employ good scientific practices from an early stage. This is enabled through making scientifically rigorous methodologies accessible and easily understandable. This study, and the literature on statistical education contain several suggestions for how this can be achieved.

One of the most well supported findings is to teach statistics grounded in real research, enabling students to feel the subject is tangible rather than theoretical (Williams, McCutcheon, Fava, & Aruguete, 2017). Such a method was used in the present study, with both the theory and the misconception tied to a practical example. Making the subject more easily understandable can also counter students’ dislike of statistics, which may encourage students to spend more time grappling with difficult concepts (Huynh & Baglin, 2017).

Another important consideration is the number of statistics teachers who hold misconceptions (Haller & Krauss, 2002). Training teachers to spot and correct their own misconceptions could prevent them being passed to students, and so is an important step in addressing the issue (Khazanov & Prado, 2010). However, it is not immediately clear how this could be achieved as correcting misconceptions is the very challenge this study attempts to address.

Problematically, $p$ value misconceptions currently persist despite many statistics courses already being grounded in research, and the plethora of resources which offer in depth explanations of topics (Earley, 2014; Greenland et al., 2016). It is therefore worth considering that the main issue may not be a lack of education, but the complexity of $p$ values themselves.

**A broken paradigm**

$P$ values are complicated to understand. The fact that this and similar papers exist is testament to that. When misconceptions persist into published work, the issue is far more serious and threatens to undermine the content and reputation of psychology (Armstrong, 2007; Hubbard & Armstrong, 2006; Meehl, 1967). Researchers and journal editors should not be making such errors, but some fault may lie with the methods themselves. Even Fisher struggled to explain the inferential meaning of $p$ values despite having practically created them (Goodman, 2008).

There are many ways to reach a $p$ value, and researchers have to make many decisions throughout an analysis (Gelman & Loken, 2013). This means that analyses quickly lose transparency and become difficult for authors to communicate and for readers to understand (Simmons, Nelson, & Simonsohn, 2011). Some of these issues can be avoided by calculating effect sizes and confidence intervals instead of $p$ values, or altering the language and processes we use in analyses (Cumming, 2008, 2014; Hurlbert & Lombardi, 2009). But such solutions do not address the root cause of the problem, namely the complexity of frequentist statistics.

Simplifying statistics could increase the transparency of research, reduce the number of incorrectly reported findings, and reduce the susceptibility of psychologists to misconceptions. As this paper has already alluded to, another school of statistics exists, one that seems to fill all of these criteria: Bayesian statistics.
Moving forwards

Although not known to most, Bayesian statistics have a longer history in scientific investigation than frequentist methods (McGrayne, 2011). Where frequentist statistics consider each analysis as one of an infinite number of notional (i.e. imaginary) replications, Bayesian methods update the probabilities of hypotheses as more data becomes available, making them more dynamic and useable. The underlying theory is simple: ‘given the data observed, how likely is this hypothesis to be true?’ The theoretical benefits of Bayesian statistics are numerous (Wagenmakers, Marsman, et al., 2018), but perhaps the most relevant advantage is their simplicity.

This study considers the misconception that a p value is the probability of the research hypothesis being true, which is precisely the correct way to interpret a Bayes factor (Kline, 2013). Bayes factors are intuitive and represent what many researchers want p values to be (Kruschke & Liddell, 2018). This intuitiveness is advantageous in avoiding misconceptions and fits well with the cognitive biases humans have towards simple explanations (Chater & Vitanyi, 2003; Lombrozo, 2007). It is difficult to see why so much time should be devoted to frequentist statistics, especially when learning so often comes at the expense of a basic awareness of Bayesian methods (Kline, 2013).

Relatively little research investigates misconceptions held about Bayesian statistics. Although I would expect them to be far less prevalent, such misconceptions could be easily investigated by applying the methods used in this and related papers. This would be a helpful step in informing reforms to statistical education.

Frequentist and Bayesian methods can also be successfully taught in concert, emphasising the differences between them (Greenland & Poole, 2013). Indeed, this has recently been incorporated into the British Psychological Society’s teaching guidance on undergraduate research methods courses (British Psychological Society, 2017). This enables students to see that there are options in statistical analysis, creating well-informed scientists.

Bayesian methods are already becoming more popular in published work (van de Schoot, Winter, Ryan, Zondervan-Zwijnenburg, & Depaoli, 2017; Wagenmakers, 2007). As this shift occurs, it makes sense for undergraduate education to do the same, so that students can understand and eventually contribute to the literature.

Conclusion

Misconceptions regarding p values have been shown to be prevalent in psychologists of all levels, which is concerning given their prevalence in published work. This study found that corrective videos did not reduce students’ misconceptions about what p values represent, and that repeating the misconception had no effect on the efficacy of the correction.

It is not immediately apparent how a more effective correction could be devised. Instead, the issue may lie with a scientific education that leaves students without sufficient statistical knowledge to dispute misconceptions. Reforming education is a drastic but necessary step to address these misconceptions. The literature provides some suggestions as to how this could be done, however the main obstacle may be the complexity of frequentist statistics themselves.

An alternative statistical method both for general use and undergraduate education is Bayesian; the result of a Bayesian analysis being what the majority of students think a p value is. This intuitiveness combined with the theoretical benefits and the ease of communicating such methods makes it difficult to argue against their use. Their inclusion in statistics classrooms has the potential to benefit students, teachers, and the discipline more broadly. Such a prospect is exciting to any true scientists – those who prize the rigorous methods of their investigations above the rewards that come
from the content of their findings. To paraphrase Dickens (1932/1859, p. 384), it is a far, far better test that I go to than I have ever been shown.

References


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